CB - 476

## 17 <br> II Semester B.C.A. Examination, August/September 2023 <br> (CBCS) (Repeaters) (2014-15 and Onwards) <br> COMPUTER APPLICATIONS

## BCA 205 : Numerical and Statistical Methods

Time: 3 Hours
Instruction : Answer all the Sections.
SECTION - A
I. Answer any ten of the following :

Max. Marks : 100

$(10 \times 2=20)$

1) Define Roundoff Error.
2) Write the formula for secant method.
3) Write the Langrange's interpolation method.
4) Write the formula for Newton's Raphson method.
5) Construct a forward difference table for the following data :

| $\mathbf{X}$ | 0 | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{Y}$ | 8 | 11 | 9 | 15 | 6 |

6) Write the Simpson's $\left(\frac{1}{3}\right)^{\text {rd }}$ formula.
7) Write the Newton's Backward interpolation method.
8) Explain Gauss-elimination method for system of linear equation.
9) Find the geometric mean of the following series $16,625,256,81$.
10) Find the median of the following data $10,15,9,25,19$.
11) Write the alternate formula for Karl Pearson's coefficient of correlation.
12) Define conditional probability.
SECTION - B
II. Answer any six of the following :
13) Find the root of the equation $x^{3}-7 x+5=0$ by using bisection method in 6 stages.
14) Estimate $f(7.5)$ from the table :

| $\mathbf{x}$ | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | 1 | 8 | 27 | 64 | 125 | 216 | 343 | 512 |

15) Using Langrange's formula find $f(10)$ from the following data:

| $\mathbf{x}$ | 5 | 6 | 9 | 11 |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{f ( x )}$ | 12 | 13 | 14 | 16 |

16) Evaluate $\int_{0}^{6} \frac{\mathrm{dx}}{1+\mathrm{x}^{2}}$ by Trapezoidal rule.
17) Evaluate $\int_{0}^{6} \frac{d x}{1+x}$ by Simpson's $\left(\frac{3}{8}\right)^{\text {th }}$, rule.
18) Solve by Gauss-Jacobi method $x+2 y+z=3,2 x+3 y+3 z, 3 x-y+2 z=13$.
19) Solve the system of equation by Crout's $L U$ decomposition method.
$x_{1}+x_{2}+x_{3}=1,4 x_{1}+3 x_{2}-x_{3}=6,3 x_{1}+5 x_{2}+3 x_{3}=4$.
20) Determine the machine representation of the decimal number 492.234375 in both single precision and double precision.

## SECTION - C

III. Answer any six of the following :
21) Solve the system of equation by Gauss elimination method.
$x+y+z=9,2 x+y-z=0,2 x+5 y+7 z=52$
22) Solve by Gauss-Seidal method $10 x+y+z=12, x+10 y+z=12$, $x+y+10 z=12$.
23) Find the largest eigen value of the matrix $A=\left[\begin{array}{ll}5 & 4 \\ 1 & 2\end{array}\right]$.
24) Solve $\frac{d y}{d x}=x^{2}+y^{2}, y(0)=1$ by Picard's method.
25) Using Taylor's series find the solution of $x \frac{d y}{d x}=x-y, y(2)=2$ at $x=2.1$ correct to five decimal places.
26) Solve $\frac{d y}{d x}=x+y$ with initial condition $y=1$ when $x=0$ when $x=0.2$ using Runge Kutta method.
27) Find the mean from the following method by shortcut method.

| Marks | 30 | 40 | 50 | 60 | 70 | 80 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of Students | 8 | 12 | 20 | 10 | 6 | 4 |

28) Compute Harmonic mean of the following series:

| $\mathbf{x}$ | 6 | 7 | 8 | 9 | 10 | 11 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{f}$ | 4 | 6 | 9 | 5 | 2 | 8 |

SECTION - D
IV. Answer any four of the following :
29) Compute the standard deviation of the following data:

| $\mathbf{X}$ | 43 | 48 | 65 | 57 | 31 | 60 | 37 | 48 | 78 | 54 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

30) Calculate Karl Pearson's coefficient of correlation between the age and weight of the children.

| Age | 1 | 2 | 3 | 4 | 5 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Weight (kg) | 3 | 4 | 6 | 7 | 12 |

31) Calculate the rank correlation of the following :

| $\mathbf{x}$ | 4 | 2 | 7 | 5 | 3 | 1 | 8 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{y}$ | 8 | 3 | 6 | 5 | 1 | 2 | 7 | 4 |

32) State and prove Baye's theorem.
33) Find the probability that in a family of 4 children there will be
i) Atleast one boy
ii) Atleast one boy and atleast one girl.
34) A die is thrown twice and the sum of the number appearing is observed to be 6 . What is the conditional probability that the number 4 has appeared at least once ?
