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IV Semester B.Sc. Examination, August/September 2023 (CBCS) (Repeaters) (2018 – 19 and Onwards) STATISTICS

Paper - IV: Statistical Inference - II

Time: 3 Hours

Max. Marks: 70

Instructions: 1) Answer any 10 sub-divisions from Section – A and any five questions from Section – B.

2) Scientific calculators are allowed.

SECTION - A

Answer any 10 sub-divisions of the following:

 $(10 \times 2 = 20)$

- 1. a) Define alternative hypotheses.
 - b) What do you mean by randomized test?
 - c) Write the test statistic for testing equality of proportions.
 - d) Give the test statistic for equality of two means.
 - e) State the assumptions involved in F-test.
 - f) Write the expression for χ^2 -test statistic used in testing independence of attributes in a (2 × 2) contingency table.
 - g) In what way parametric test is different from non-parametric test?
 - h) Explain the test for randomness.
 - i) Mention sign test statistic for one sample.
 - j) Define runs. Find the number of runs from the following sequence :
 PPPFPFFFPPP
 - k) Write the test statistic used in Spearman's rank correlation coefficient in NP test.
 - I) What is the need for sequential test?



SECTION - B

Answer any five questions from the following:

 $(5 \times 10 = 50)$

2. a) Given the following function:

$$f(x, \theta) = \begin{cases} \frac{1}{\theta}, & 0 \le x \le \theta \\ 0, & \text{otherwise} \end{cases}$$

Find the probabilities of type I and II errors and power of the test for testing the hypothesis $H_0: \theta = 1$ Vs $H_1: \theta = 2$, if the critical region is $X \le 0.5$.

b) State Neyman Pearson lemma.

(7+3)

- 3. a) The hypothesis $H_0: \theta=2$ is accepted against $H_1: \theta=5$ if $x\leq 3$ when X has an exponential distribution with mean θ . Find type I and type II error probabilities of the test.
 - b) Define most powerful test.

(7+3)

- 4. a) Explain the test procedure for testing equality of means of two normal populations with equal variances.
 - b) Explain the test procedure for testing $H_0: P = P_0 \ Vs \ H_1: P \neq P_0$ where P is the binomial population proportions. (5+5)
- 5. a) Explain the χ^2 test of goodness of fit.
 - b) Discuss 'F' test for testing multiple correlation coefficient.

(5+5)

- 6. a) Explain the χ^2 test of independence of attributes.
 - b) Describe the test procedure for testing regression coefficient.

(5+5)

- 7. a) Explain paired 't' test.
 - b) Explain Yate's correlation.

(5+5)

- 8. a) Describe Wilcoxon signed rank test for paired samples.
 - b) Explain median test.

(5+5)

- 9. a) Describe SPRT for testing H_0 : $\mu = \mu_0$ Vs H_1 : $\mu = \mu_1$ for $N(\mu, \sigma^2)$ distribution.
 - b) Describe SPRT for testing n and p of B(n, p).

(5+5)