

BCA 105T: Discrete Mathematics

Time: 3 Hours

Max. Marks: 100

LIBRARY

 $(10 \times 2 = 20)$

Instruction: Answerall Sections.

SECTION - A



- 1) Define a power set. Illustrate with an example.
- 2) If $P = \{1, 2\}$ form the $P \times P \times P$.
- 3) Define equivalence relation.
- 4) Define Scalar Matrix with example.

5) If
$$A = \begin{pmatrix} 2 & 1 \\ 4 & -2 \end{pmatrix}$$
, $B = \begin{pmatrix} 4 & 3 \\ 2 & -1 \end{pmatrix}$ find AB.

- 6) Prove that $3 \log 2 + \log 5 = \log 40$.
- 7) Define permutation.
- 8) Define Coplanar vectors.
- 9) Define slope of a line.
- 10) Find the equation of the straight line passing through (2, 5) and having slope 4.
- 11) Find the coordinates of the mid point which divides the join of (4, 3) and (-2, 7).
- 12) Define order of a group.

SECTION - B

II. Answerany six of the following:

 $(6 \times 5 = 30)$

- 13) Verify whether $(p \rightarrow q) \leftrightarrow (\neg q \rightarrow \neg p)$ is a tautology.
- 14) Prove that $\sim (p \leftrightarrow q) = \sim [(p \rightarrow q) \land (q \rightarrow p)]$.
- 15) Consider $f: R \rightarrow R$ given by f(x) = 4x + 3. Show that f is invertible.

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- 16) Verify Cayley Hamilton theorem for the matrix $A = \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix}$.
- 17) Solve using Cramer's rule

$$3x + y + z = 3$$

$$2x + 2y + 5z = -1$$

$$x - 3y - 4z = 2$$

- 18) Solve the equations 2x + 5y = 1, 3x + 2y = 7 using matrix method.
- 19) Find the eigen values and eigen vectors of $A = \begin{pmatrix} 1 & 4 \\ 3 & 2 \end{pmatrix}$.
- 20) Let $A = Z^+$, the set of positive integers. $R = \{(a, b) \mid a \le b\}$. Is R an equivalence relation.

SECTION - C

III. Answerany six of the following:

 $(6 \times 5 = 30)$

21) If
$$\log x - 2\log \frac{6}{7} = \frac{1}{2}\log \frac{81}{16} - \log \frac{27}{196}$$
 find x.

- 22) a) Find the number of different signals that can be generated by arranging atleast 3 flags in order (one below the other) on a vertical staff, if 6 different flags are available.
 - b) If $\frac{1}{9!} + \frac{1}{10!} = \frac{x}{11!}$ find x.
- 23) a) Find r if ${}^{10}P_r = 2^9p_r$
 - b) In how many ways can the letters of the word ASSASSINATION be arranged so that all the S's are together.
- 24) A committee of 7 has to be formed from 9 boys and 4 girls. In how many ways can this be done when the committee consist of (i) exactly 3 girls (ii) atleast 3 girls (iii) atmost 3 girls.
- 25) Prove that $G = \{1, 5, 7, 11\}$ is a group under multiplication modulo 12.
- 26) If $\vec{a} = \hat{i} 2\hat{j} + 3\hat{k}$ and $\vec{b} = 2\hat{i} + 3\hat{j} 5\hat{k}$ find $\vec{a} \times \vec{b}$. Verify that \vec{a} and $(\vec{a} \times \vec{b})$ are perpendicular to each other.
- 27) Prove that $\vec{a} \times (\vec{b} \times \vec{c}) + \vec{b} \times (\vec{c} \times \vec{a}) + \vec{c} \times (\vec{a} \times \vec{b}) = 0$.
- 28) Using vector method show that the points A (2, -1, 3), B (4, 3, 1) and C (3, 1, 2) are collinear.

SECTION - D

IV. Answerany four of the following:

 $(4 \times 5 = 20)$

- 29) Prove that the points (4, -4), (8, 2), (14, -2) and (10, -8) are the vertices of a square.
- 30) Find the equation of the locus of the point which moves such that its distance from (0, 3) is twice its distance from (0, -3).
- 31) Show that the line joining the points (2, -3) and (-5, 1) is
 - a) Parallel to the line joining (7, -1) and (0, 3)
 - b) Perpendicular to the line joining (4, 5) and (0, -2).
- 32) Find the equation of the straight line which passes through the point of intersection of the lines 3x + y 10 = 0 and x + 7y 10 = 0 and parallel to the line 4x 3y + 1 = 0.
- 33) Find the equations of the straight lines passing through the point (4, -2) and making an angle of $\frac{\pi}{4}$ with the line 8x + 7y 1 = 0.
- 34) Prove that points (2, 2) and (-3, 3) are equidistant from the line x + 3y 7 = 0 and are on either side of the line.