



CS – 172

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V Semester B.Sc. Examination, March 2023
(CBCS) (2019-20 and Onwards) (F+R)
STATISTICS – V

Sampling Theory and Statistical Quality Control

Time : 3 Hours



Max. Marks : 70

- Instructions :** 1) Answer **any five** questions from Section – A and **any five** questions from Section – B.
2) Scientific calculator is **allowed**.

SECTION – A

- I. Answer **any five** of the following questions. (5×5=25)
- 1) Distinguish between Sampling errors and Non sampling errors.
 - 2) Obtain an expression for sample size while estimating population mean in case of SRSWOR.
 - 3) Discuss proportional and optimum allocation in stratified random sampling.
 - 4) What is systematic sampling ? In a linear systematic sampling prove that systematic sample mean is an unbiased estimator of the population mean.
 - 5) Derive the control limits for \bar{X} and S chart, when process standards are unknown.
 - 6) Discuss any five criteria to detect lack of control on control chart.
 - 7) Briefly explain the construction of control limits for 'np' chart.
 - 8) Define AQL and LTPD.

SECTION – B

- II. Answer **any five** of the following questions. (5×9=45)
- 9) a) Explain principle steps in conducting a sample survey.
b) Explain the advantages of sample survey over a complete enumeration. (4+5)
 - 10) a) Prove that $N\bar{y}_n$ is an unbiased estimator of population total in SRSWOR.
b) Compare the variances of SRSWR and SRSWOR. (4+5)

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- 11) a) Explain the simple random sampling for proportions and with usual notations find the expression for $V(\hat{A})$

where $\hat{A} = Np$

p = proportion of sampled units possessing the given attribute.

- b) Obtain the expression for sample size while estimating population proportions in simple random sampling. **(4+5)**
- 12) In stratified random sampling show that the variance of the estimate of the population mean is minimum if n_h is proportional to $\frac{N_h S_h}{\sqrt{C_h}}$ $h = 1 \dots l$ and hence obtain the expression for $V(\bar{y}_{st})$. **9**

- 13) a) With usual notations prove that in linear systematic sampling variance of sample mean is given by

$$V(\bar{y}_{sys}) = \frac{(N-1)S^2}{N} - \frac{(n-1)K}{N} S_{wsys}^2$$

- b) Discuss advantages and disadvantages of systematic sampling. **(5+4)**
- 14) a) Discuss the advantages and disadvantages of control charts for variables and control charts for attributes.
- b) Explain the construction of control limits for 'U' chart. **(4+5)**
- 15) a) Explain :
- i) Producer's risk
 - ii) Consumer's risk
 - iii) AOQ
 - iv) ASN.
- b) Obtain the expression for O.C. and ATI of a Single Sampling Plan (SSP). **(4+5)**
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