V Semester B.Sc. Examination, January/February 2025 (NEP) (Freshers/Repeaters) **STATISTICS**

Paper – V: Sampling Theory and Regression Analysis

Time: 21/2 Hours

Max. Marks: 60

Instructions: i) Scientific calculators are **permitted**.

ii) Statistical tables and graph sheets are provided on request.

PART - A

Answer any four questions (2 marks each):

 $(2 \times 4 = 8)$

- 1. Define sample with an example.
- 2. What do you mean by Standard Error (S.E.)?
- 3. Define Simple Random Sampling (SRS).
- 4. With usual notations, prove that E(p) = P.
- 5. Mention any two merits of systematic sampling.
- 6. What do you mean by regression?



PART - B

Answer any four questions (5 marks each).

 $(5 \times 4 = 20)$

- 7. Explain the types of sampling.
- 8. Prove that the probability of selecting a specified unit of a population at any given draw is equal to the probability of its being selected at the first draw. i.e., $p(E_r) = p(E_1)$.
- 9. Explain the lottery system method of drawing a sample.
- 10. Prove that $E(\overline{y}_{st}) = \overline{y}_{N}$.

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- 11. Explain systematic sampling and mention its important notations and terminologies.
- 12. Give the test procedure for testing $H_0: \beta_1 = \beta_{10}$ of $Y = \beta_0 + \beta_1 X$.

Answer any four questions (8 marks each):

 $(8 \times 4 = 32)$

- 13. Explain the sampling and non-sampling errors.
- 14. In SRSWOR, prove that sample mean square is an unbiased estimate of the population mean square i.e. $E(S^2) = S^2$.
- 15. a) Distinguish between SRSWOR and SRSWR.
 - b) Explain the advantages and disadvantages of SRS.

(2+6)

- 16. Under proportional allocation derive an expression for n_i . Also find the $V(\overline{y}_{st})$ under proportional allocation.
- 17. With usual notations prove that in linear systematic sampling variance of sample mean is given by $Var(\overline{y}_{sys}) = \frac{N-1}{N} \cdot S^2 \frac{(n-1)K}{N} \cdot S^2_{wsy}$ where $S^2_{wsy} = \frac{1}{K(n-1)} \sum_{i=1}^k \sum_{j=1}^n \left(y_{ij} \overline{y}_i \right)^2 \text{ is the mean square among units which lie within the same systematic sample.}$
- 18. Derive the simple linear regression equation.